

L5 MATHEMATICS ASSIGNMENTS

16) Give that $f(x) = \frac{1}{2}x^2e^{x+1}$

- a) Find the domain of $f(x)$, (1 marks)
- b) Find relative asymptotes (if any), (4 marks)
- c) Study the first and second derivative with variation table, (8 marks)
- d) Sketch the curve of $f(x)$. (2 marks)

02. Given the function $f(x) = \frac{1}{x-2} + 2$

- a) Find domain of definition and boundary limits 4marks
- b) Find asymptotes to the curve 2marks
- c) Compute the first derivative and study its sign 2marks
- d) Compute the second derivative and study its sign 2marks
- e) Find the variation table 2marks
- f) Sketch the graph of the curve in Cartesian plane 3marks

3. Given the function $f(x) = e^x - 1$

- a. Find the domain of definition of $f(x)$ [1mark]
- b. Find Asymptotes to the curve [2marks]
- c. Find the limits at boundaries of domain of definition [2marks]
- d. Compute the first derivative and study its sign [2marks]
- e. Compute the second derivative and study its sign [2marks]
- f. Make a variation table [2marks]
- g. Find intercept points with the axes [2marks]
- h. Sketch the graph of the function [2marks]

04. Given the function $f(x) = \ln(2x+3)$:

- a) Find the domain of definition of $f(x)$ [3marks]
- b) Calculate limit at boundaries of the domain of definition; [3marks]
- c) Find both x and y -intercepts; [3marks]
- d) Find the first derivative of $f(x)$ and its table of signs; [3marks]
- e) Find the second derivative of $f(x)$ and its table of signs. [3marks]

05.

$$\text{Let } f(x) = \frac{x^2-1}{x^2-4}$$

- a) Determine the domain of definition of this function (2marks)
- b) Calculate the limits around the boundaries of the domain found in a) and deduce the equations of all possible asymptotes. (2marks)
- c) Find the coordinates of intersection points of the asymptotes to the curves. (1mark)
- d) Study the variations and draw the variation table (7marks)
- e) Sketch the graph of the curve representing f . (3marks)